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## Some Types of Ideal on Supra Topological Space

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### ABSTRACT

**Background:** This paper introduces some types of ideals on supra topological space called  $I^*$ ,  $I^{**}$ ,  $\alpha I^*$  &  $\alpha I^{**}$ , and it is studying the relations among ideal,  $I^*$  and  $I^{**}$ ,  $\alpha I^*$  &  $\alpha I^{**}$ , on supra topological space. Also introduce a new class of sets and functions between topological space called supra  $\alpha I^*$ -open sets and supra  $\alpha I^{**}$ -open sets. Finally investigate some properties between them.

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## INTRODUCTION

(Vaidyanathswamy, 1960) and (Kuratowski, 1966) introduced the concept of ideal topological space. (Shyamapada Modak and Sukalyan Mistry, 2012) defined local function in ideal supra topological space. Further Shyamapada Modak and Sukalyan Mistry studied the properties of ideal supra topological space and they have introduced three operator called  $(\cdot)^{\mu}$ ,  $\psi_{\mu}$  and  $\psi_{\mu} - C$  sets. (Modak and Bandyopadhyay, 2007) have defined generalized open sets using  $\psi$  - operator. More recently (AI-Omri and Noiri, 2012) have defined the ideal m-space and introduced two operators as like similar to the local function and  $\psi$  - operator. Different types of generalized open sets like semi-open (N. Levine, 1963), preopen (A.S. Mashhur, M.E. Abd El-Monsef and I.A. Hasanein, 1984), semi per open (D. Andrijevic, 1986),  $\alpha$ -open (O. Njastad, 1965), I - semi continuity points (T. Natkaniec, 1986) already are there in literature and these generalized sets have a common property which is closed under arbitrary union. (Mashhour, 1983) put all of the sets in a pocket and defined a generalized space which is supra topological space. This paper introduces some types of ideals on supra topological space called  $I^*$ ,  $I^{**}$ ,  $\alpha I^*$  &  $\alpha I^{**}$ , and it is studying the relations among ideal,  $I^*$  and  $I^{**}$ ,  $\alpha I^*$  &  $\alpha I^{**}$ , on supra topological spaces. Also introduce a new class of sets and functions between topological spaces called supra  $\alpha I^*$ -open sets and supra  $\alpha I^{**}$ -open sets. Finally investigate some properties between them.

### Preliminaries:

In this section we introduced some definitions and results which are need of this paper.

#### Definition 2.1:

(K. Kuratowski, 1966) : A nonempty collection  $I$  of subsets of  $X$  is called an ideal on  $X$  if :

- (i).  $A \in I$  and  $B \subset A$  implies  $B \in I$  (heredity) ;
- (ii).  $A \in I$  and  $B \in I$  implies  $A \cup B \in I$  (finite additivity).

#### Definition 2.2:

(A.S. Mashhour, A. A. Allam, F. S. Mahmoud and F. H. Khedr, 1983) A sub family  $\mu$  of the power set  $P(X)$  of a nonempty set  $X$  is called a supra topology on  $X$  if  $\mu$  satisfies the following conditions:

1.  $\mu$  contains  $\phi$  and  $X$ ,

2.  $\mu$  is closed under the arbitrary union.

The pair  $(X, \mu)$  is called a supra topological space. In this respect, the member of  $\mu$  is called supra open set in  $(X, \mu)$ . The complement of supra open set is called supra closed set.

**Definition 2.3:**

(M.Shyamapada and M.Sukalyan, 2012) We called the triple of  $(X, \mu, I)$  ideal supra topological space if  $(X, \mu)$  is supra topological space and  $I$  is ideal on  $X$ , and we use  $(X, I)$  instead of  $(X, \mu, I)$  for simply.

**Definition 2.4:**

(M.Shyamapada and M. Sukalyan, 2012) Let  $(X, \mu)$  be a supra topological space and  $A \subset X$ . Then supra interior and supra closure of  $A$  in  $(X, \mu)$  defined as

$$\cup \{ U : U \subseteq A, U \in \mu \} \text{ and } \cap \{ F : A \subseteq F, X - F \in \mu \} \text{ respectively.}$$

The supra interior and supra closure of  $A$  in  $(X, \mu)$  are denoted as  $Int^\mu(A)$  and  $Cl^\mu(A)$  [13] respectively. From definition,  $Int^\mu(A)$  is a supra open set and  $Cl^\mu(A)$  is a supra closed set.

**Definition 2.5:**

(M.Shyamapada and M.Sukalyan, 2012) Let  $(X, \mu)$  be a supra topological space and  $M \subset X$ . Then  $M$  is said to a supra neighborhood of a point  $x$  of  $X$  if for some supra open set  $U \in \mu, x \in U \subset M$ .

**Theorem 2.6:**

(M.Shyamapada and M.Sukalyan, 2012) Let  $(X, \mu)$  be a supra topological space and  $A \subset X$ . Then

- (i).  $Int^\mu(A) \subseteq A$ .
- (ii).  $A \in \mu$  if and only if  $Int^\mu(A) = A$ .
- (iii).  $Cl^\mu(A) \supseteq A$ .
- (iv).  $A$  is a supra closed set if and only if  $Cl^\mu(A) = A$ .
- (v).  $x \in Cl^\mu(A)$  if and only if every supra open set  $Ux$  containing  $x$ ,  $Ux \cap A \neq \phi$ .

**Theorem 2.7:**

(M.Shyamapada and M.Sukalyan, 2012) Let  $(X, \mu)$  be a supra topological space and  $A \subset X$ . Then  $Int^\mu(A) = X - Cl^\mu(X - A)$ .

**Definition 2.8:**

(A. S. Mashhour, A. A. Allam, F. S. Mahmoud and F. H. Khedr, 1983): We called the triple of  $(X, \mu, I^*), (X, \mu, I^{**})$  respectively, ideal supra topological space if  $(X, \mu)$  is supra topological space and  $I^*$  (resp.  $I^{**}$ ) on  $X$  is *ideal\** (resp. *ideal\*\**) on  $X$ .

Now, our work introduce two concepts of  $I^*$  &  $I^{**}$  on supra topological space.

**Definition 2.9:**

A nonempty collection  $I$  of subsets of  $X$  is called  $I^*$  on  $X$  if

- (i).  $A \in I$  and  $B \subset A$  implies  $B^c \in I$ ;
- (ii).  $A \in I$  and  $B \subset A$  implies  $(A \cup B)^c \in I$ .

**Definition 2.10:**

A nonempty collection  $I$  of subsets of  $X$  is called  $I^{**}$  on  $X$  if

- (i).  $A \in I$  and  $B \subset A$  implies  $B^c \in I$  ;  
 (ii).  $A \in I$  and  $B \subset A$  implies  $(A \cap B)^c \in I$  .

Now we study the relations among them ideal,  $I^*$  and  $I^{**}$  .

**Remark 2.11:**

The following relation are independent .

ideal  $\nrightarrow I^*$  &  $I^* \nrightarrow$  ideal

**Example 2.12:**

Let  $X = \{a, b, c, d\}$ ,  $I = \{\{a\}, \{b, c\}, \{c\}, \{a, c\}\}$ ,  $A = \{a, c\}$ .

$B = \{a\}$  . Then  $(X, I)$  is ideal because satisfies two conditions of ideal , but is not  $(X, I^*)$  because  $(A \cup B)^c \notin I$  .

**Example 2.13:**

Let  $X = \{a, b, c\}$ ,  $I = \{\{a\}, \{b, c\}, X\}$ ,  $A = \{b, c\}$ ,  $B = \emptyset$  . Then  $(X, I^*)$  satisfies two conditions of  $I^*$ , but  $(X, I)$  is not ideal because  $B \notin I$  .

**Remark 2.14:**

The following relation are independent.

ideal  $\nrightarrow I^{**}$  &  $I^{**} \nrightarrow$  ideal

**Example 2.15:**

Let  $X = \{a, b, c\}$ ,  $I = \{\{a\}, \{c\}, \{a, c\}\}$ ,  $A = \{a, c\}$ ,  $B = \{a\}$  . Then  $(X, I)$  is ideal because satisfies two conditions of ideal, but is not  $(X, I^{**})$  because  $(A \cap B)^c \notin I^{**}$  .

**Example 2.16:**

Recall Example 2.12 we see that  $(X, I^{**})$  satisfies two conditions of  $I^{**}$ , but  $(X, I)$  is not ideal because  $B \notin I$  .

**Remark 2.17:**

The following relation are independent .

$I^* \rightarrow I^{**}$  &  $I^{**} \nrightarrow I^*$

**Proposition 2.18:**

Every  $(X, I^*)$  is  $(X, I^{**})$  .

**Proof:**

suppose  $(X, I^*)$  and  $A \in I$  ,  $B \subset A$  implies  $B^c \in I$  . Since  $(A \cup B)^c \in I$  then  $A^c \cap B^c \in I$ , since every  $A \cap B \subseteq A \cup B$  then  $A^c \cup B^c \supseteq A^c \cap B^c$  .

So that  $(A \cap B)^c \in I$  . Therefore  $(X, I^{**})$  is satisfy.

**Remark 2.19:**

The converse of Proposition 2.18 is not true in general.

The counter example show the converse is not true .

**Example 2.20:**

Let  $X = \{a, b, c\}$ ,  $I = \{\{a\}, \{b, c\}, \{a, c\}\}$ ,  $A = \{a, c\}$ ,

$B = \{a\}$  . Then  $(X, I^{**})$  satisfies two conditions of  $I^{**}$ , but  $(X, I^*)$  is not satisfy because  $(A \cup B)^c \notin I$  .

**Basic properties of supra  $\alpha I^*$ -open sets:**

In this section we introduce a new class of sets .

**Definition 3.1:**

Let  $(X, \mu, I^*)$  be an ideal supra topological space. A set  $A^c$  is called supra  $\alpha I^*$ -open set if  $\text{supra int}(\text{supra cl}(A^c)) \subseteq A^c$ .

**Proposition 3.2:**

Every ideal supra open set is supra  $\alpha I^*$ -open set

**Proof:**

Let  $A^c$  be an ideal supra open set in  $(X, \mu, I^*)$ . Since  $A^c \supseteq \text{supra cl}(A^c)$ , then  $\text{supra int}(A^c) \supseteq \text{supra int}(\text{supra cl}(\text{supra int}(A^c)))$ .

Hence  $A^c \supseteq \text{supra int}(\text{supra cl}(\text{supra int}(A^c)))$ .

**Remark 3.3:**

The converse of the above proposition need not be true. This is shown by the following example.

**Example 3.4:**

Let  $(X, \mu, I^*)$  be an ideal supra topological space. Where  $X = \{a, b, c\}$  and  $\mu = \{\phi, X, \{a\}\}$ . Then  $\{a, c\}$  is a supra  $\alpha I^*$ -open set, but not ideal supra open.

**Proposition 3.5:**

Every supra  $\alpha I^*$ -open set is ideal supra semi-open set.

**Proof:**

Let  $A^c$  be a supra  $\alpha I^*$ -open set in  $(X, \mu, I^*)$ . Therefore,  $\text{supra int}(\text{supra cl}(\text{supra int}(A^c))) \subseteq A^c$ . It is obvious that,  $\text{supra cl}(\text{supra int}(A^c)) \subseteq \text{supra int}(\text{supra cl}(\text{supra int}(A^c)))$ . Hence  $\text{supra cl}(\text{supra int}(A^c)) \subseteq A^c$ .

**Remark 3.6:**

The converse of the above proposition need not be true. This is shown by the following example.

**Example 3.7:**

Let  $(X, \mu, I^*)$  be an ideal supra topological space. Where  $X = \{a, b, c\}$  and  $\mu = \{\phi, X, \{a\}\}$ . Then  $\{b, c\}$  is ideal supra semi open set, but not  $\alpha I^*$ -open .

**Proposition 3.8:**

Finite union of ideal supra  $\alpha I^*$ -open sets is always ideal supra  $\alpha I^*$ -open set.

**Proof:**

Let  $A^c$  and  $B^c$  be two supra  $\alpha I^*$ -open sets. Then  $\text{supra int}(\text{supra cl}(\text{supra int}(A^c))) \subseteq A^c$  and  $\text{supra int}(\text{supra cl}(\text{supra int}(B^c))) \subseteq B^c$ , this implies,  $\text{supra int}(\text{supra cl}(\text{supra int}(A^c \cup B^c))) \subseteq A^c \cup B^c$ . Therefore  $A^c \cup B^c$  is supra  $\alpha I^*$ -open set.

**Remark 3.9:**

Finite intersection of ideal supra  $\alpha I^*$ -open sets may fail to be ideal supra  $\alpha I^*$ -open set .

**Example 3.10:**

Let  $(X, \mu, I^*)$  be an ideal supra topological space. Where  $X = \{a, b, c\}$  and  $\mu = \{\phi, X, \{a\}, \{a, b\}\}$ . Then  $\{a\}, \{a, b\}$  are supra  $\alpha I^*$ -open sets, but their intersection is a not supra  $\alpha I^*$ -open set.

**Definition 3.11:**

Complement of ideal supra  $\alpha I^*$ -open is a supra  $\alpha I^*$ -closed set.

**Proposition 3.12:**

(i) Finite intersection of ideal supra  $\alpha I^*$ -closed sets is always a supra  $\alpha I^*$ -closed set.

**Proof:**

(i) This follows immediately from Proposition 3.8.

**Remark 3.13:**

Finite union of ideal supra  $\alpha I^*$ -closed set may fail to be supra  $\alpha I^*$ -closed set.

**Example 3.14:**

Let  $(X, \mu, I^*)$  be an ideal supra topological space. Where  $X = \{a, b, c, d\}$  and  $\mu = \{\phi, X, \{a\}, \{a, b\}\}$ . Then  $\{a, d\}, \{c, d\}$  are supra  $\alpha I^*$ -closed sets, but their union is not a supra  $\alpha I^*$ -closed set.

**Definition 3.15:**

The supra  $\alpha I^*$ -closure of a set  $A^c$  is denote by supra  $\alpha I^*$  cl( $A^c$ ) and defined as, supra  $\alpha I^*$  cl( $A^c$ ) =  $\cap \{B^c : B^c \text{ is ideal supra } \alpha I^* \text{-closed set and } A^c \subseteq B^c\}$ .

The supra  $\alpha I^*$ -interior of a set is denoted by supra  $\alpha I^*$  int( $A^c$ ), and defined as ,supra  $\alpha I^*$  int( $I^*$ ) =  $\cup \{B^c : B^c \text{ is ideal supra } \alpha I^* \text{-closed set and } B^c \subseteq A^c\}$ .

**Remark 3.16:**

It is clear that supra  $\alpha I^*$  int( $A^c$ ) is a supra  $\alpha I^*$ -open set and supra  $\alpha I^*$  cl( $A^c$ ) is a supra  $\alpha I^*$ -closed set.

**Proposition 3.17:**

- (i)  $X - \text{supra } \alpha I^* \text{ int}(A^c) = \text{supra } \alpha I^* \text{ cl}(X - A^c)$ .
- (ii)  $X - \text{supra } \alpha I^* \text{ cl}(A^c) = \text{supra } \alpha I^* \text{ int}(X - A^c)$ .

**Proof:**

(i) and (ii) are clear from Definition 3.15 and Remark 3.16.

**Proposition 3.18:**

The following statements are true for every  $A^c$  and  $B^c$ .

- (1)  $\text{supra } \alpha I^* \text{ int}(A^c) \cup \text{supra } \alpha I^* \text{ int}(B^c) = \text{supra } \alpha I^* \text{ int}(A^c \cup B^c)$
- (2)  $\text{supra } \alpha I^* \text{ cl}(A^c) \cap \text{supra } \alpha I^* \text{ cl}(B^c) = \text{supra } \alpha I^* \text{ cl}(A^c \cap B^c)$ .

**Proof:**

Obvious.

**Basic properties of supra  $\alpha I^{**}$ -open sets:**

In this section we introduce a new class of sets.

**Definition 4.1:**

Let  $(X, \mu, I^{**})$  be an ideal supra topological space. A set  $A^c$  is called supra  $\alpha I^{**}$ -open set if  $\text{supra int}(\text{supra cl}(A^c)) \subseteq A^c$ .

**Proposition 4.2:**

Every ideal supra open set is supra  $\alpha I^{**}$ -open set

**Proof:**

The prove is same as prove Proposition 3.2.

**Remark 4.3:**

The converse of the above proposition need not be true. This is shown by the following example.

**Example 4.4:**

Let  $(X, \mu, I^{**})$  be an ideal supra topological space. Where  $X = \{a, b, c\}$  and  $\mu = \{\phi, X, \{b, c\}\}$ . Then  $\{a\}$  is a supra  $\alpha I^{**}$ -open set, but not ideal supra open.

**Proposition 4.5:**

Every supra  $\alpha I^{**}$ -open set is ideal supra semi-open set.

**Proof:**

The prove is same as prove Proposition 3.5

**Remark 4.6:**

The converse of the above proposition need not be true. This is shown by the following example.

**Example 4.7:**

Let  $(X, \mu, I^{**})$  be an ideal supra topological space. Where  $X = \{a, b, c\}$  and  $\mu = \{\phi, X, \{b\}\}$ . Then  $\{a, c\}$  is ideal supra semi open set, but not  $\alpha I^{**}$ -open.

**Proposition 4.8:**

Finite intersection of ideal supra  $\alpha I^{**}$ -open sets is always ideal supra  $\alpha I^{**}$ -open set.

**Proof :**

Let  $A^c$  and  $B^c$  be two supra  $\alpha I^{**}$ -open sets. Then  $\text{supra int}(\text{supra cl}(\text{supra int}(A^c))) \subseteq A^c$  and  $\text{supra int}(\text{supra cl}(\text{supra int}(B^c))) \subseteq B^c$ , this implies,  $\text{supra int}(\text{supra cl}(\text{supra int}(A^c \cap B^c))) \subseteq A^c \cap B^c$ . Therefore  $A^c \cap B^c$  is supra  $\alpha I^{**}$ -open set.

**Remark 4.9:**

Finite union of ideal supra  $\alpha I^{**}$ -open sets may fail to be ideal supra  $\alpha I^{**}$ -open set.

**Example 4.10:**

Let  $(X, \mu, I^{**})$  be an ideal supra topological space. Where  $X = \{a, b, c\}$  and  $\mu = \{\phi, X, \{a\}, \{a, c\}, \{b\}\}$ . Then  $\{a\}, \{a, b\}$  are supra  $\alpha I^{**}$ -open sets, but their intersection is not supra  $\alpha I^{**}$ -open set.

**Definition 4.11;**

Complement of ideal supra  $\alpha I^{**}$ -open is a supra  $\alpha I^{**}$ -closed set.

**Proposition 4.12:**

(i) Finite union of ideal supra  $\alpha I^{**}$ -closed sets is always a supra  $\alpha I^{**}$ -closed set.

**Proof:**

(i) This follows immediately from Proposition 4.8.

**Remark 4.13:**

Finite intersection of ideal supra  $\alpha I^*$ -closed set may fail to be supra  $\alpha I^*$ -closed set .

**Example 4.14:**

Let  $(X, \mu, I^{**})$  be an ideal supra topological space. Where  $X = \{a, b, c\}$  and  $\mu = \{\phi, X, \{a, b\}\}$ . Then  $\{a, c\}, \{b, c\}$  are supra  $\alpha I^*$ -closed set but their union is not a supra  $\alpha I^{**}$ -closed set .

**Definition 4.15:**

The supra  $\alpha I^{**}$ -closure of a set  $A^c$  is denote by supra  $\alpha I^* \text{cl}(A^c)$  and defined as, supra  $\alpha I^{**} \text{cl}(A^c) = \cap \{B^c : B^c \text{ is ideal supra } \alpha I^{**} \text{-closed set and } A^c \subseteq B^c\}$ .

The supra  $\alpha I^{**}$ -interior of a set is denoted by supra  $\alpha I^{**} \text{int}(A^c)$ , and defined as ,supra  $\alpha I^{**} \text{int}(A^c) = \cup \{B^c : B^c \text{ is ideal supra } \alpha I^{**} \text{-closed set and } B^c \subseteq A^c\}$ .

**Remark 4.16:**

It is clear that supra  $\alpha I^{**} \text{int}(A^c)$  is a supra  $\alpha I^{**}$ -open set and supra  $\alpha I^{**} \text{cl}(A^c)$  is a supra  $\alpha I^{**}$ -closed set .

**Proposition 4.17:**

- (i)  $X - \text{supra } \alpha I^{**} \text{int}(A^c) = \text{supra } \alpha I^{**} \text{cl}(X - A^c)$  .
- (ii)  $X - \text{supra } \alpha I^{**} \text{cl}(A^c) = \text{supra } \alpha I^{**} \text{int}(X - A^c)$  .

**Proof:**

(i) and (ii) are clear from Definition 4.15 and Remark 4.16.

**Remark 4.18:**

The following statements are true for every  $A^c$  and  $B^c$  .

- (1) supra  $\alpha I^{**} \text{int}(A^c) \cup \text{supra } \alpha I^{**} \text{int}(B^c) \neq \text{supra } \alpha I^{**} \text{int}(A^c \cup B^c)$
- (2) supra  $\alpha I^{**} \text{cl}(A^c) \cap \text{supra } \alpha I^{**} \text{cl}(B^c) \neq \text{supra } \alpha I^{**} \text{cl}(A^c \cap B^c)$ .

**Example 4.19:**

Let  $(X, \mu, I^{**})$  be an ideal supra topological space. Where  $X = \{a, b, c\}$  and  $\mu = \{\phi, X, \{a, b\}, \{b\}\}$ . Then supra  $\alpha I^{**} \text{int}(A^c) = \{a, c\}$ , supra  $\alpha I^{**} \text{int}(B^c) = \{a, b\}$  and supra  $\alpha I^{**} \text{int}(A^c \cup B^c) = \{a, c\}$ . We see that supra  $\alpha I^{**} \text{int}(A^c) \cup \text{supra } \alpha I^{**} \text{int}(B^c) = \{a, b, c\} \neq \{a, c\} = \text{supra } \alpha I^{**} \text{int}(A^c \cup B^c)$  .

Thus supra  $\alpha I^{**} \text{int}(A^c) \cup \text{supra } \alpha I^{**} \text{int}(B^c) \neq \text{supra } \alpha I^{**} \text{int}(A^c \cup B^c)$  .

**Example 4.20:**

Let  $(X, \mu, I^{**})$  be an ideal supra topological space. Where  $X = \{a, b, c, d\}$  and  $\mu = \{\phi, X, \{a, b\}, \{b, d\}, \{b\}\}$ . Then supra  $\alpha I^{**} \text{int}(A^c) = \{a, b, d\}$ , supra  $\alpha I^{**} \text{int}(B^c) = \{a, c\}$  and supra  $\alpha I^{**} \text{int}(A^c \cap B^c) = \{a, d\}$ . We see that supra  $\alpha I^{**} \text{int}(A^c) \cap \text{supra } \alpha I^{**} \text{int}(B^c) = \{a\} \neq \{a, c\} = \text{supra } \alpha I^{**} \text{int}(A^c \cap B^c)$  .

Thus supra  $\alpha I^{**} \text{cl}(A^c) \cap \text{supra } \alpha I^{**} \text{cl}(B^c) \neq \text{supra } \alpha I^{**} \text{cl}(A^c \cap B^c)$ .



## REFERENCES

- Al-Omari, A. and T. Noiri, 2012. "On  $\psi^*$ -operator in ideal  $m$ -spaces", Bol. Soc. Paran. Mat. (3s) v.30 1 53-66, ISSN-00378712 in press.
- Andrijevic, D., 1986. "Semi-preopen sets", Mat. Vesnik, 38: 24-32.
- Kuratowski, K., 1966. "**Topology**", Vol.1 Academic Press, New York.
- Levine, N., 1963. "Semi-open sets and semi-continuity in topological spaces", Amer. Math. Monthly, 70: 36-41.
- Mashhur, A.S., M.E. Abd El-Monsef and I.A. Hasanein, 1984. "On pre topological Spaces", Bull. Math. R.S. Roumanie (N.S) 28(76)1, 39-45.
- Mashhour, A.S., A.A. Allam, F.S. Mahmoud and F.H. Khedr, 1983. "On supra topological spaces", Indian J. Pure and Appl. Math., 14(4): 502-510.
- Modak, S. and C. Bandyopadhyay, 2007. "A note on  $\psi$  – operator", Bull. Malyas. Math. Sci. Soc., (2) 30 (1).
- Shyamapada, M. and M. Sukalyan, 2012. "Ideal on Supra Topological Space", Int. Journal of Math. Analysis, 6(1): 1-10.
- Natkaniec, T., 1986. "On  $I$ -continuity and  $I$  – semicontinuity points", Math. Slovaca, 36(3): 297-312.
- Njastad, O. 1965. "On some classes of nearly open sets", Pacific J. Math, 15: 961-970.
- Vaidyanathaswamy, R., 1960. "**Set topology**", Chelsea Publishing Company.