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## A Comparative Analysis of Optical Flow Algorithms for Velocimetry

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### ABSTRACT

The use of an optical method for velocimetry is important where it is not possible to use invasive flow measurement techniques, as is the case in a hydrocarbon leak from a ruptured subsea pipeline. However, measurements of the velocity of fluids optically is inherently difficult due to dense fluid motion and lack of distinct features. Timothy J. Crone (Crone et al, 2008) developed a system based on optical plume velocimetry, an optical flow technique, to determine flow rates using image analysis. In this paper, the performance of three optical flow algorithms, iterative Lucas-Kanade, Horn-Schunck and Brox based on warping theory, for optical plume velocimetry were assessed. Crone's experimental setup was replicated and the accuracy of the three algorithms at three different flow rates were assessed. The Brox optical flow algorithm, based on theory of warping, was the most accurate, with an average error of 8.6%.

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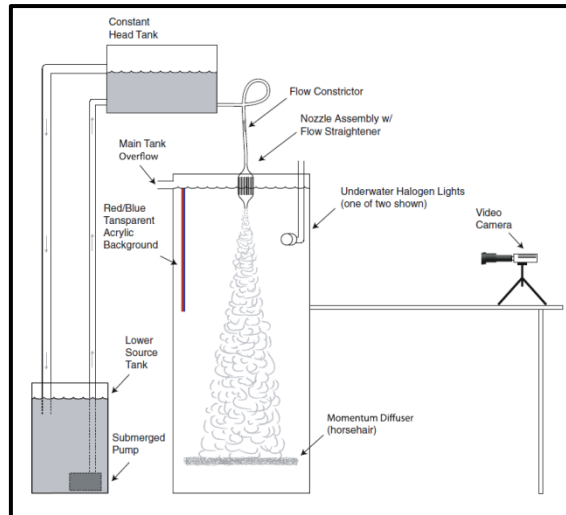
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## INTRODUCTION

As the oil and gas industry ventures further deep water to keep up with the world's energy demand, leaks from ruptured pipelines are inevitable, despite tight safety measures. An accurate estimate of the leak flow rate is necessary as interventions are based on the flow rate. A recent example is the Deepwater Horizon oil spill on April 20, 2010 in the Gulf of Mexico at an approximate water depth of 1500 metres (Command, 2011). The tragedy which caused the death of 11 workers and millions of barrel of spilled oil. It is regarded as the largest accidental marine oil spill in the history of the industry. There was a dispute between the well operator, BP and the United States Government on the amount of spilled oil, since there were no proven methods in accurately predicting its volume. Various ad hoc methods were employed to predict the flow rate of hydrocarbon escaping from the leakage, with the most accurate method that by Crone et al (Crone, McDuff, & Wilcock, 2008) using an optical flow based on optical plume velocimetry.

### Methodology:

Crone's (Crone, McDuff, & Wilcock, 2008) experimental setup, as shown in Figure 1, was replicated to simulate an oil leak for optical flow measurement (Suffian, 2014). There are two tanks used in the setup, a lower tank filled with water, and an upper tank containing a mixture of water and graphite, used to replicate black smoker phenomenon in deepwater. The lower tank was filled with water until the nozzle was submerged in water. The upper tank was filled with water until it reached 150mm head. An aqueous-based colloidal dispersion of ultra-fine graphite, Aquadag®, was used to simulate hydrocarbon fluid. The valve is then opened fully to allow the graphite solution flow through the nozzle and the flow of graphite solution is recorded by using a video camera. This step is repeated for a 50% opening and a 25% opening of the valve.



**Fig. 1:** Experiment Setup(Crone, McDuff, & Wilcock, 2008).

A total of 9 videos were analysed, 3 videos each for 100%, 50%, and 25% nozzle opening. The camera specifications used for video recording was as shown in Table 1.

**Table 1:** Camera Properties.

Camera Model	Nikon Coolpix L820
Effective Pixels	16 Million
Sensor Size	1/2.3"
Video Recording	Full HD: 1920x1080p
Frame Rate	30fps
ISO Sensitivity	ISO125-1500;ISO3200(Auto Mode)

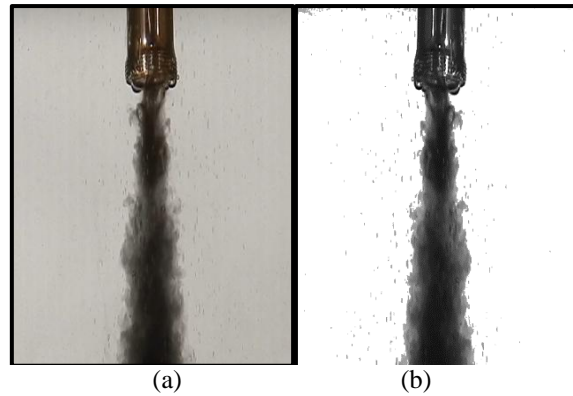
**Video Analysis:**

The raw data produced from the video were RGB images. A sample image for a 100% valve opening is shown in Figure 2.



**Fig. 2:** An RGB image of the flow at 100% valve opening extracted from a video recording.

The image was cropped to the size of 480p x 640p of the jet region. The cropped image is shown in Figure 3.



**Fig. 3:** Cropped sample RGB image (a) and the corresponding Kittler-Illingworth thresholded image (b).

Several thresholding algorithm that were considered such as Bradley's Adaptive Thresholding (Bradley, 2006), Gray Image Thresholding using Triangle Method, and Kittler-Illingworth (Kittler, 1986). Kittler-Illingworth thresholding algorithm was chosen as it manages to preserve the profile of the fluid flow while eliminating noise in the image. The thresholding of Kittler-Illingworth's come from a mixture of two normal distributions having mean and variances, and their respective proportions. It models the two resulting pixel populations, foreground and background, one from those pixels whose brightness level is smaller than threshold and the other with the higher value than the threshold. The value of threshold chosen is based on a value which minimizes the criterion function of the image, automatically giving a recommended threshold level of a given image. The threshold level for the sample image using this method was a grayscale level of 171 and the resultant image is shown in Figure 3. As can be seen, the thresholded image retains most of the profile of the flow while eliminating the background noise.

#### Optical Flow:

The flow rate (pixel/frame) was determined based on several optical flow algorithms applied to the thresholded images. The algorithms included in this study are Iterative Lucas-Kanade, Horn-Schunk and Brox based on Warping Theory. The resulting flow rate will be compared to the actual flow rate obtained from volume of fluid displaced over time. Table 2 shows the experimental results. The example shown for the conversion of flow rate to velocimetry (p/f) was for 100% valve opening. The summary of all actual flow rate was shown in Table 3.

**Table 2:** Experimental Flow Rates.

No	Valve Opening (%)	Displaced height, $h$ (cm)	Area, $A$ (cm <sup>2</sup> )	Time Taken, $t$ (s)
1	100	0.5	5625	120
2	50	0.4	5625	120
3	25	0.3	5625	120

$$V_D = A \times h \quad (1)$$

where,  $V_D$ = Displaced Volume (cm<sup>3</sup>),  $A$  = Area of Container (cm<sup>2</sup>),  $h$  = Displaced height (cm)

$$\therefore V_D = 5625 \text{ cm}^2 \times 0.5 \text{ cm} = 2812.5 \text{ cm}^3$$

$$\dot{V} = \frac{V_D}{t} \quad (2)$$

where,  $\dot{V}$  = Volumetric flow rate (cm<sup>3</sup>/s),  $V_D$ = Displaced Volume (cm<sup>3</sup>),  $t$  = time taken (s)

$$\therefore \dot{V} = \frac{2812.5 \text{ cm}^3}{120 \text{ s}} = 23.43 \text{ cm}^3/\text{s}$$

As the radius of nozzle is 0.8cm, the marker besides the nozzle serve as an indicator to determine the relationship between pixels and the length. It was determined that 72 pixels are equivalent to one centimetre. The camera used in the experiment had the speed of 30 frame/s as shown in Table 1. Thus, the velocimetry (p/f) can be calculated by using the given information.

$$r = 0.8 \text{ cm}$$

$$1 \text{ cm} = 72 \text{ pixels}$$

$$v_{f/s} = 30 \text{ frame/s}$$

$$v = \frac{\dot{V}}{A_{\text{nozzle}}} \quad (3)$$

where,  $v$ = fluid velocity (cm/s),  $\dot{V}$ = Volumetric flow rate (cm<sup>3</sup>/s),  $A_{\text{nozzle}}$  = Cross-sectional area of nozzle (cm<sup>2</sup>)

$$\therefore v = \frac{23.43 \text{ cm}^3/\text{s}}{\pi(0.8^2)} = 11.65 \text{ cm/s}$$

$$v_{p/f} = \frac{v}{\alpha v_{f/s}} \quad (4)$$

where,  $v_{p/f}$  = velocimetry (pixel/frame),  $v$  = fluid velocity (cm/s),  $\alpha$  = centimetre per pixel constant (cm/pixel),  $v_{f/s}$  = speed of camera (frame/s)

$$\therefore v_{p/f} = \frac{11.05 \text{ cm/s}}{\left(\frac{1 \text{ cm}}{72 \text{ pixels}}\right)(30 \text{ frame/s})} = 27.9 \text{ p/f}$$

**Table 3:** Flow rate.

No.	Nozzle Opening (%)	Volumetric Flow Rate, $\dot{V}$ (cm <sup>3</sup> /s)	Fluid Velocity, $v$ (cm/s)	Velocimetry, $v_{p/f}$ (p/f)
1.	100	12.5	11.7	26.5
2.	50	10.5	9.3	22.4
3.	25	7.9	7.0	16.7

#### **Iterative Lucas-Kanade Optical Flow Algorithm:**

The iterative Lucas-Kanade(Bouguet, 2001) is a feature tracking based algorithm which has the two key elements of accuracy and robustness. The accuracy component is related to the accuracy of local sub-pixel assigned to be tracked. In order to avoid smoothing the details of the images, a small integration window is need to preserved details in the images. However, the robustness component need a large integration window for better tracking sensitivity with respect to lighting and the image size. Hence, iteration is needed to balance the size of integration window for an optimum result. The feature selection in the algorithm is generalized in 5 steps(Bouguet, 2001) which are:

1. Compute the size of the image and its minimum eigenvalue at every pixel of the image.
2. Set the maximum eigenvalue in the image as the general eigenvalue for the whole image.
3. Retain the image pixel (tracked object) that is within the eigenvalue.
4. Retain the local maximum pixel of the retained feature.
5. Retain the subset of the pixel so that the minimum distance between pair of pixels is larger than threshold distance.

#### **Horn-Schunck Optical Flow Algorithm:**

Horn-Schunck(Corpetti, Heitz, Arroyo, & Memin, 2005) is a variational-based algorithm, capable of extracting the dense motion field of a fluid flow. The computation of its velocimetry is based on spatiotemporal derivatives of image intensity, with assumption of continuous image domain in space and time. The algorithm takes the whole image into account in estimating the vectorial continuous function representing velocity field. The technique is able to overcome the limitation of a feature-based algorithm, such as loss of the features due to the incorrect interrogation window, bias towards the lower displacements and higher seeded sub-regions as a result of more frequent pairing, with only the most probable displacement extracted for interrogation.

#### **Warping Theory:**

Warping theory by Brox(Brox, Bruhn, Papenberg, & Weickert, 2004) is a variational-based algorithm with improvement over the Horn-Schunck algorithm. Warping theory uses variational-based algorithm smoothness assumption to provide spatiotemporal continuity in the image domain. The algorithm implements non-linearized optical flow constraint integration using a warping technique. Complementing the grey value constancy assumption is the gradient constancy assumption in order to make the algorithm robust to the changes in grey values. Gradient constancy assumption is important when there are changes in the grey values due to the aperture changes.

#### **Results:**

Several thresholding algorithm had been applied and tested. The thresholding algorithm by Kittler was found to be the most suitable. The summary of the accuracy of the resultant algorithms are shown in Table 4. The Lucas-Kanade optical flow algorithm has the highest average error of 38.1%, followed by Horn-Schunck with an average error of 24.7%, and Brox based on warping theory with the lowest average error of 8.6%. As the Lucas Kanade algorithm is based on feature-based matching, which recognize the boundary of an object with regards to the background, these profile were processed with the next frame of image and translated to velocimetry. It consistently produce the least accurate results for all three nozzle openings, as shown in Table 4. As such, feature-based matching algorithm is not suitable for fluid flow due to the flow profile. Horn-Schunck

and Warping Theory is a variational-based algorithm which uses smoothness for the resulting flow field to provide continuity in the image domain. The approaches compute the optical flow field for all pixels within the image, and the resultant is a dense optical flow field.

**Table 4:** Comparison of Optical Flow Algorithms for Flow Rate Estimation.

No	Optical Flow Algorithms	Mean Error (%)			Average Error (%)
		100% Nozzle Opening	50% Nozzle Opening	25% Nozzle Opening	
1	Lucas-Kanade(Bouguet, 2001)	36.9	45.7	31.8	38.1
2	Horn-Schunk(Corpetti, Heitz, Arroyo, & Memin, 2005)	21.7	29.9	22.4	24.7
33	Brox (Warping Theory)(Brox, Bruhn, Papenberg, & Weickert, 2004)	2.3	13.4	10.1	8.6

Brox, which is based on warping theory, is a variation al-based algorithm as it incorporates a gradient constancy assumption for the robustness of the algorithm. As shown in Table 4, it has the best accuracy of all three algorithms considered. However further study should be done to investigate the effect of smoothness constant in variation al-based algorithms. To measure the flow rate of hydrocarbon leakage, the actual deep water conditions e.g. high pressures and low temperatures, need to be replicated. In addition, video recordings will be susceptible to sway due to sea current; resulting in slight changes in the angle of view, which will affect the overall accuracy. Thus, the effect of sway should be considered for robustness. Additionally, the usage of high speed camera would be beneficial to the development of the system, as the flow rate could be in estimated more accurately, albeit at the expense of computation cost as there will be vast amount of information to be processed.

#### **Conclusion:**

A comparative analysis of three optical flow algorithms for optical plume velocimetry was performed at three different flow rates to investigate the accuracy of each algorithm. The three optical flow algorithms investigated were Iterative Lucas-Kanade, Horn-Schunk, and Brox based on warping theory. Of the three algorithms considered, the Brox optical flow algorithm, based on theory of warping, was the most accurate, with an average error of 8.6%.

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